TEMPERATURE DEPENDENCE OF THE ELECTRON AND HOLE MEAN FREE PATHS IN ANTIMONY

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The temperature dependences of the mean free paths for electrons and holes in antimony are measured separately on the basis of the amplitudes of the radio frequency size effect lines. In both cases the temperature-dependent part of the path was found to be proportional to T^{-2}, the proportionality coefficient for holes being three times greater than that for electrons. It is shown that if the Fermi surface resembles a long, narrow cylinder, the term quadratic with respect to temperature in the carrier scattering probability may be ascribed to interaction between electrons and phonons and that it is precisely this case which is encountered in bismuth and antimony. The magnitudes of the deformation potentials in antimony are estimated for both electrons and holes.

So far there is rather little information concerning the connection between the cross section for scattering of electrons in a metal and their position on the Fermi surface. Kinetic processes widely used for the investigation of electron relaxation times, such as electric or thermal conductivity, are determined by quantities averaged over the entire Fermi surface. At the same time, there already exist methods for separating and investigating individual groups of carriers in a metal. Such methods include, in particular, the measurement of the amplitude of the lines of the radio frequency size effect (SE).[1,2] The SE line is formed by electrons located in the vicinity of a definite extremal section of the Fermi surface. Therefore the line amplitude is determined by the probability of scattering of precisely these electrons.

The purpose of the experiments described here was to compare the cross sections for the scattering of the carriers of both types by phonons, using one sample of antimony (in one experiment), by measuring the temperature dependence of the amplitude of the SE lines from the electronic and hole parts of the Fermi surface.

EXPERIMENT

An antimony sample in the form of a disk of thickness d = 0.32 mm and diameter 10 mm was grown from the melt in a dismountable quartz mold. The initial material was antimony with a resistance ratio $\rho_{room}/\rho_{4.2°K} \approx 2700$. The angles between the normal to the plane of the sample and the axes C_2 and C_3 were 46°10′ and 44°20′. The experiments were performed in the temperature range from 1.17 to 4.2°K. The amplitudes of the SE lines were measured on the plots of the derivatives, with respect to the magnetic field, of the imaginary part of the surface impedance, $\partial X/\partial H$ or $\partial^2 X/\partial H^2$, at a frequency 12.5 MHz. We used the usual modulation procedure for the measurements—see, for example, [1]. To record the second derivative, the detecting part of the apparatus was tuned to a frequency equal to double the modulation frequency,

A considerable line width ($\Delta H/H \approx \delta/d \approx 15\%$; δ—

depth of skin layer) made it necessary to take into account in the data reduction the monotonic part of the function $\partial X/\partial H$. There was no monotonic part in the second derivative, but this did not lead to an appreciable increase of the measurement accuracy. Sample plots are shown in Fig. 1.

As is well known,[3] the Fermi surface of antimony consists of three electron and six hole surfaces of nearly-ellipsoidal shape. The number of hole surfaces that cannot be made congruent by parallel transfers in k-space is only 3, and each pair of surfaces capable of being made congruent gives one SE line.

We observed the SE lines from the three electron surfaces and two pairs of hole surfaces. Within the limits of the experimental accuracy, the dimensions which we succeeded in measuring, and the slopes of the surfaces relative to the crystallographic axes, fully coincide with those indicated in [3] The deviations of the projections of the Fermi surfaces on the plane of the sample from ellipticity, while noticeable (especially for the hole surfaces), were at the borderline of the accuracy of our experiments. To measure these deviations, we propose to carry out in the future a special series of experiments on samples with different orientations. For the time being, in discussing all the experimental meas-
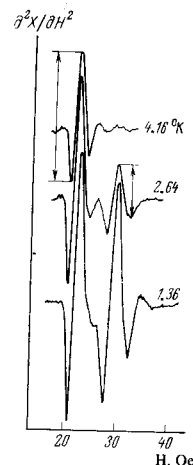

FIG. 1. Sample plots of SE lines for antimony. The left line in the lower plots pertains to the hole ellipsoid, for which $\psi = 30°$, and the right one to the electronic ellipsoid, which lies in the plane of the sample ($\xi = 37°$). The arrows show the value chosen for the line amplitude in this plot.

urements of the free paths, we used a quadratic model with the following values of the principal semiaxes of the ellipsoids and cyclotron masses at the minimal cross sections[3] (k is in cm^{-1}):

	$10^{-7} k_1$	$10^{-7} k_2$	$10^{-7} k_3$	$m_c^{\min}/m_0$
Holes:	0.42	0.45	1.4	0.069
Electrons:	0.42	0.50	2.7	0.084

To measure the mean free path l with the aid of the SE it is necessary to know the path length Λ of the electron from one surface of the plate to the other. In the general case Λ is a rather complicated function of the angles, which may, furthermore, depend strongly on small deviations of the Fermi surface from ellipticity. If, however, the magnetic field H and the major semi-axis of the ellipsoid k_3 lie in the plane of the sample, then, recognizing that for electrons and holes $k_1 \approx k_2 \ll k_3$, we can use the formula $\Lambda = \pi d/2$ in a large interval of angles ξ between H and k_3. This formula is valid up to those values of ξ for which we can neglect the deviation of the Fermi surface from cylindrical shape. For a circular cylinder whose axis makes an angle ψ with the surface of the metal we have $\Lambda = \pi d/2 \cos \psi$, regardless of the value of the angle ξ ($\xi \neq \pi/2$). In this connection, all the main measurements were performed on one of the electron ellipsoids and on one of the pairs of hole ellipsoids, for which $\psi \lesssim 5°$.

If the electron traverses the path Λ between the two sides of the plate only once, then the line amplitude is $A \propto \exp -\Lambda/l$ and

$$\ln A(T) = \text{const} - \frac{\Lambda}{l} = \text{const} - \frac{\pi d}{2}\left(\frac{1}{l_0} + \frac{T^n}{\beta}\right). \quad (1)$$

The measurement results processed in accordance with this formula gave for the function $l_T = (l^{-1} - l_0^{-1})^{-1} = \beta T^{-n}$ the values (see Fig. 2)

$$l_T{}^{el} = 0.22/T^2 \ [\text{cm}] \quad l_T{}^h = 0.68/T^2 \ [\text{cm}] \quad (2)$$

(here and throughout T is in degrees K and l_0 is the mean free path at T = 0). For the hole ellipsoid, the value of β was measured at 12 points in the angle interval from 20 to 70°. The scatter of the values of β was limited to ±7%. For the electron ellipsoid, the angle interval was $35° \leq \xi \leq 80°$ and the scatter ±12%. It was impossible to perform measurements at smaller angles ξ, owing to the overlap of the lines from different ellipsoids. (Even the plots of Fig. 1 show a partial overlap, but measurements of A(T) are still possible if one uses for A the dimensions indicated in the figure by arrows.)
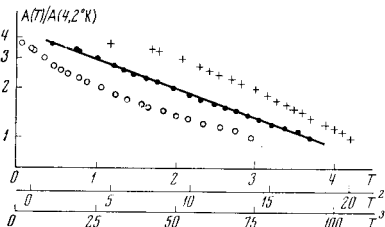

FIG. 2. Reduced amplitude of the SE line from the hole ellipsoid (in logarithmic scale) as a function of T (points +), T^2 (points ●), and T^3 (points ○). We see that the filled points fit the straight line well. Its slope gives the value of β, see (1).

Since the electron can, generally speaking, execute several revolutions on the trajectory, it is more accurate to write in place of (1) the sum

$$A(T) = C \sum_{\nu=1}^{\infty} e^{-\nu\Lambda/l} = C(e^{\Lambda/l} - 1)^{-1} = C[\eta \exp(\pi dT^n/2\beta) - 1]^{-1}, \quad (3)$$

where $C = A(0)$ ($\eta = 1$) and $\eta = \exp(\pi d/2 l_0)$. From (3) we obtain the expression

$$\ln\left(\frac{C}{A(T)} + 1\right) = \frac{\pi d}{2 l_0} + \frac{\pi d}{2}\beta^{-1}T^n, \quad (4)$$

in which, unlike in (1), the logarithm contains the parameter C, defined by the value of l_0. A reduction of the experimental data by means of formula (4), even with C corresponding to $l_0 = 0.3$ mm, did not lead to a change of the exponent n. The coefficient β increased at this value of C by 15%. Larger values of l_0 have low probability, since no SE was observed on samples 0.5 mm thick, made of the same material, down to the lowest temperatures.

DISCUSSION

Since the experimentally obtained degree T^2 is characteristic of the contribution of electron-electron scattering, we first make some estimates of the probability of the electron-electron collision.

To this end we use the formula for the differential cross section for the scattering of an electron from the state **k** to the state **k**' by a screened potential in the form $U(r) = (e^2/\kappa r) \exp -gr$ (κ is the static dielectric constant and g^{-1} the Debye radius; see [4] Ch. 6):

$$d\sigma = \left(\frac{2me^2}{\kappa\hbar^2}\right)^2 (|\mathbf{k} - \mathbf{k}'|^2 + g^2)^{-2}.$$

If it is recognized that the Fermi wave vector is $k_F \approx g$ both for an ordinary metal ($k_F \approx g \approx 1/a$, where a is the interatomic distance) and for a semimetal (in bismuth $k_F \approx g \approx 100/a$, and in antimony $k_F \approx g \approx 10/a$), then the total scattering cross section at $\mathbf{k} = k_F$ is expressed in terms of the Fermi energy ϵ_F:

$$\sigma = 16\pi \left(\frac{me^2}{\kappa\hbar^2}\right)^2 [g^2(4k_F^2 + g^2)]^{-1} \approx \left(\frac{e^2}{\kappa\epsilon_F}\right)^2. \quad (5)$$

Multiplying by the number of scatterers, taking into account the limitations imposed by the Pauli principle on the possible collisions in the electron gas, we obtain for the mean free path l_{ee}

$$l_{ee}^{-1} \approx \sigma \frac{1}{N_e}\left(\frac{\partial N_e}{\partial \varepsilon}\right)^2_{\varepsilon=\varepsilon_F} (k_B T)^2, \quad l_{ee} \approx N_e\left(\frac{\kappa}{e^2}\right)^2 \left(\frac{\partial N_e}{\partial \varepsilon}\right)^{-2}_{\varepsilon_F}\left(\frac{\varepsilon_F}{k_B T}\right)^2 \quad (6)$$

(N_e is the total number of electrons per unit volume and k_B is Boltzmann's constant).

For antimony, $N_e = 10^{20}$ cm^{-3}, $\partial N_e/\partial \epsilon \approx 10^{33}$ erg^{-1} cm^{-3},[5] $\kappa \approx 100$,[6] and $l_{ee} \approx 10/T^2$. We see therefore that the coefficient of T^{-2} exceeds by 10 times the corresponding value from our measurements of l_T. Furthermore, as is known from calculations for sodium,[7] the estimate obtained for l_{ee} from (6) is underestimated by several times because of numerical factors. The entire further discussion will therefore be devoted to electron-phonon interaction.

For an isotropic electron dispersion law, the value of l_T measured with the aid of the SE and determined

by the scattering of the electrons by the phonons should be proportional to

$$l_\tau \propto T^{-5} \quad \text{for} \quad q_\tau / k_F \ll \delta/d \ll 1, \tag{7}$$

$$l_\tau \propto T^{-3} \quad \text{for} \quad \delta/d \ll q_\tau / k_F \ll 1 \tag{8}$$

($q_T = k_B T/\hbar s$, s is the speed of sound; depending on the type of the SE, the inequalities (7) and (8) may contain other expressions in lieu of δ/d—for details see [2]),

$$l_\tau \propto T^{-1} \quad \text{for} \quad q_\tau / k_F \gtrsim 1 \tag{9}$$

(the high-temperature case; under these conditions, however, the SE is no longer observed).

In (8) and (9), the measured value of l_T is the true path length traversed by the electron between two collisions with phonons ($l_T = l_{e,ph}$). Of course, the experimentally obtained relation $l_T \propto T^{-2}$ can be regarded as a transition from (8) to (9), since at $4°$K $q_T \approx 0.3 \times 10^7$ cm^{-1} in antimony (compare with the values of k_1 listed in the table above). However, as indicated in [8], in the case of a sharply anisotropic electron dispersion law the relation $l_{e,ph} \propto T^{-2}$ should be obtained in a definite rather broad temperature interval.

Indeed, we shall use a model in which the probability of scattering of an electron with a wave vector K is given by the expression

$$\frac{v}{l_{e,ph}} = \frac{\Delta^2}{8\pi^2 NMs} \int q[n_q(1-f_{K+q})\delta(\varepsilon_K + \hbar qs - \varepsilon_{K+q}) + (n_q+1)(1-f_{K-q})\delta(\varepsilon_K - \hbar qs - \varepsilon_{K-q})]d^3q. \tag{10}$$

Here Δ is the deformation potential, M the mass of the lattice ions, N the number of atoms per unit volume, v the electron velocity, and n_q and f_{K+q} are the occupation numbers for the phonons and electrons; the two terms in the square brackets take into account respectively the absorption and production of the phonon, the integration is carried out over all wave vectors q, and the δ function ensures satisfaction of the conservation laws (see [4], Ch. 5). The deformation potential, generally speaking, is a tensor quantity: $\Delta_{ij}(k)$. In our experiments, however, we measured the total scattering of the electrons by phonons of all polarizations, and the effect of the action of different phonons was automatically averaged. It is therefore natural to regard Δ as a scalar quantity and to take it outside the integral sign in (10). The averaging of Δ over k occurs along the orbit of the electron in k-space, and therefore, naturally, $\Delta^{el} \neq \Delta^h$.

Let the Fermi surface be an infinite circular cylinder of radius K and, as always at low temperatures, let the conditions $\epsilon(K) \gg \hbar qs$ and $V_F \gg s$ hold. Owing to the latter inequalities, the distance Δk between two equipotential surfaces ϵ and $\epsilon + \hbar qs$ in k-space is $\Delta k = qs/v \ll q$, and it can be assumed that the electron remains after scattering on the same surface. The region of integration in q-space in (10) reduces to a cylinder of the same radius K, passing through the origin, with an axis parallel to the Fermi-cylinder axis. Indeed, the argument of the δ functions is

$$\varepsilon_K \pm \hbar qs - \varepsilon_{K\pm q} = \pm \hbar qs - \frac{\hbar^2}{2m}(q_1^2 \pm 2Kq_1 \cos\varphi) \tag{11}$$

$$\approx \frac{\hbar^2 Kq_1}{m}\left(\frac{q_1}{2K} \pm \cos\varphi\right),$$

where q_1 is that component of the vector q which is perpendicular to the cylinder axis, and φ is the angle between K and q_1. Equating the expression in the parentheses in (11) to zero, we obtain precisely the equation of a cylinder.

Expression (10) in terms of the function $f_{K\pm q}$ depends on the energy of the scattered electron, so that this expression must be averaged over the initial values of the electron energy along the normal to the Fermi surface. It is necessary to bear in mind here that the SE lines are formed only by the nonequilibrium electrons determined by the increment Δf to the equilibrium distribution function $f^{(0)}$. The value of Δf is proportional, as is well known, to the derivative $\partial f^{(0)}/\partial\epsilon$; the proportionality coefficient, which can be regarded as a constant near the Fermi surface during the course of integration along the normal to this surface, drops out upon normalization, so that it is necessary to make in (10) the substitution

$$1 - f_{K\pm q} \to -\int_0^\infty \frac{\partial f^{(0)}}{\partial\varepsilon}(1 - f^{(0)}_{K\pm q})d\varepsilon.$$

The expression in the square brackets in (10) then goes over into

$$[n_q(1-f_{K+q}) + (n_q+1)(1-f_{K-q})] \to xe^x(e^x-1)^{-2},$$
$$x = \hbar qs/k_B T,$$

and (10) is transformed into

$$\frac{v}{l_{e,ph}} = \frac{\Delta^2}{2\pi^2 NMvs\hbar}\left(\frac{k_B T}{\hbar s}\right)^3 \int_0^{y_0}\frac{dy}{\sqrt{1-(y/y_0)^2}}\int_y^\infty \frac{x^3 e^x\,dx}{\sqrt{x^2-y^2}(e^x-1)^2} \tag{12}$$

$$y_0 = 2Q/T,$$

where $Q = \hbar Ks/k_B$ is the characteristic temperature, which replaces in this problem the Debye temperature Θ.

If the cylinder is sufficiently thin so that

$$T \gg Q, \tag{13}$$

then we obtain from (12)

$$\frac{v}{l_{e,ph}} = \pi^3 \frac{\Delta^{2'}}{\hbar v s M}\left(\frac{K}{q_\Theta}\right)\left(\frac{T}{\Theta}\right)^3 = \frac{\pi}{6}\frac{\Delta^2 K^3}{\hbar v s M N}\left(\frac{T}{Q}\right)^2 \tag{14}$$

($q_\Theta^3 = 6\pi^2 N$ is the Debye wave vector). It is precisely this case which is realized in bismuth for electrons.[8] In the opposite limiting case $T \ll Q$, we obtain the same formula as for the Fermi sphere:

$$\frac{v}{l_{e,ph}} = 9\pi\zeta(3)\frac{\Delta^2}{\hbar v s M}\left(\frac{T}{\Theta}\right)^3 = \frac{3\zeta(3)}{2\pi}\frac{\Delta^2 K^3}{\hbar v s M N}\left(\frac{T}{Q}\right)^3$$
$$\zeta(3) = 1.20. \tag{15}$$

For the intermediate region of temperatures, the integral in (12) was evaluated with a computer (see Fig. 3).

Antimony falls precisely in the intermediate region. In order for the experimental points to fall in the region $l \propto T^{-2}$ on the curve of Fig. 3 (the right-hand side of the curve, corresponding to $T/Q > 1$), it would be necessary to assume that the average sound velocity is $s \lesssim 10^5$ cm/sec. This contradicts the experimental data.[9] It is more correct to assume the average value to be $s \approx 2 \times 10^5$ cm/sec. In this connection, we can note the following.

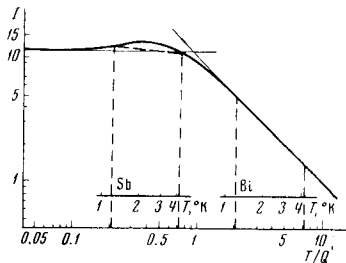In the region $T \approx Q$, a change takes place in the char-

FIG. 3. The double integral I in expression (12) as a function of the parameter T/Q. The vertical dashed lines show the measurement regions for antimony and bismuth, respectively. The scale corresponds for antimony to the sound velocity s = 2 × 10⁵ cm/sec, and for bismuth to s = 1.5 × 10⁵ cm/sec.

acter of the scattering: a major role is assumed by collisions that change the direction of the electron momentum through angles $\gamma \sim 1$. For such collisions, the matrix element of the transition in (10) should contain one more factor—a certain function of the scattering angle $G(\gamma)$ (see [4], Ch. 5). This function does not change the power-law relations in the asymptotic formulas (14) and (15). For $T \ll Q$, the function $G(\gamma = 0) = 1$ by definition, and for $T \gg Q$ the scattering is isotropic, so that the contribution of G reduces to the appearance of some additional numerical factor. But in the region $T \approx Q$ the function $G(\gamma)$ is quite capable of extending the quadratic dependence into the region of low temperatures.

Inasmuch as under the condition $T \gtrsim Q$ each act of scattering by a phonon leads to a change of the electron momentum by a large angle, formula (14) can be used directly to calculate the quantity l_ρ which enters in the electric resistivity of semimetals in the corresponding temperature range. Indeed, in [10, 11] a quadratic dependence of the temperature-dependent part of the electric resistivity of antimony on T was observed in the region from 1.5°K to hydrogen temperatures.

Let us note one peculiarity of electron-phonon scattering. As seen from formulas (12), (14), and (15), $l_{e,ph} \infty v^2$. Since the velocity along the principal directions of the ellipsoid is $v^2 = v_i^2 \infty k_i^{-2}$, the mean free path $l_{e,ph}$ for electrons located near the major semiaxes turns out to be much smaller than near the minor ones. For electrons in bismuth, for example, where $k_{max}/k_{min} \approx 14$, the ratio $l_{e,ph}^{max}/l_{e,ph}^{min}$ reaches 200. In antimony this ratio is approximately 30 for electrons and 10 for holes. (These, of course, are only estimates, since no account was taken of either the anisotropy of the phonon spectrum or of the dependence of the integration region in (12) on k.) The values of $l_{e,ph}$ measured by us for antimony, and also in [6] for electrons in bismuth, pertain to carriers with minimum values of the momentum within the limits of the given ellipsoid, i.e., close to $l_{e,ph}^{max}$.

Little is known concerning the anisotropy of l_0. From numerical estimates for the averaged value of l_0 it follows that near the points $|k| = k_{max}$ at helium temperatures the scattering by phonons prevails over the impurity scattering, and the resultant mean free path $l \approx l_{e,ph}^{min} \ll l_0$. This can probably explain why in such experiments on semi metals as the de Haas–van Alphen

effect, cyclotron resonance, or the size effect it is very difficult to observe the sections that pass through the major semiaxes of the Fermi ellipsoids.

Thus, it is quite probable that at helium temperatures $l_0 < l_{e,ph}$ for some carriers and $l_0 > l_{e,ph}$ for others. Under these conditions, strictly speaking, the electric resistivity cannot be subdivided into residual and ideal components, since the Matthiessen rule does not hold. It is therefore very difficult to compare our coefficients in (2) with the results of measurements of the electric resistance, and no great significance should be attached to the rather good agreement between our coefficients in (2) and the coefficient obtained from the data of [10, 11] from the quadratic term ρ_T in the resistance in accordance with the formula $l_\rho = \hbar K/N_e e^2 \rho_T$.

The quantities $l_{e,ph}$ measured by us make it possible to calculate the constant Δ. Putting in (14) MN = 6.7 g/cm³, s = 2 × 10⁵ cm/sec, v^{el} = 5.8 × 10⁷ cm/sec, v^h = 6.7 × 10⁷ cm/sec, and K = 4.4 × 10⁶ cm⁻¹, we obtain

$$|\Delta^{el}| = 2.9 \text{ eV}, \quad |\Delta^h| = 1.9 \text{ eV}. \tag{16}$$

These values can be compared, first, with measurements of the deformation potential as determined from the amplitude of the quantum oscillations of sound absorption:[12] by averaging the squares of the diagonal elements of the tensor Δ_{ij}, we obtain for electrons $\Delta \approx 4.1$ eV, while all that is known for holes is that the components of the tensor are smaller than those for electrons. Second, we note that the deformation potential obtained under the assumption $|\Delta^{el}| = |\Delta^h| = \Delta$ from measurements of the thermal conductivity of antimony amounts to 1.8 eV.[13]

Violation of condition (13) makes it necessary to consider the experimental values (16) as approximate. However, in view of the fact that for electrons and holes in antimony the transverse dimensions of the ellipsoids are practically the same, and the difference between the dimensions of the long semiaxes in the investigated temperature interval is negligible, since $k_B T/\hbar s \ll k_3$, the "geometric factor" connected with the integration is the same for electrons and holes. Therefore the inaccuracy of formula (14) and the uncertainty in the choice of s should not affect the ratio $|\Delta^{el}|/|\Delta^h| = 1.5$.

This ratio permits another comparison with an independent experiment. According to [14], hydrostatic compression increases the number of carriers: $\Delta N_e/N_e \approx 1\%$ per kbar. Assuming for estimating purposes

$$B \frac{\Delta N_e}{N_e} = \frac{3}{2} \frac{\Delta^h - \Delta^{el}}{E},$$

where E is the band overlap and B is the bulk modulus of elasticity (B ≈ 400 kbar), we obtain either Δ^{el} = −0.3 eV and Δ^h = 0.2 eV (the extrema shift in opposite directions at decreasing specific volume), or Δ^{el} = −1.6 eV and Δ^h = −1.0₅ eV (both extrema shift downward). The second assumption agrees much better with (16).

A similar analysis can also be carried out with respect to the results of [8] for bismuth. Although the l_{ee} calculated from (6) differs much less from the mean free path l_T measured in [8] for electrons, there is every reason for assuming that in bismuth the tempera-

ture-dependent scattering is determined by electron-phonon collisions. This is confirmed, in particular, by the character of the dependence of the coefficient of the temperature-dependent part of the electric resistivity on the carrier density in bismuth-antimony alloys.[15] The data of [8] reduced in accordance with formula (14) lead to $\Delta_{Bi}^{el} = 2.6$ eV, whereas the diagonal elements of the tensor Δ_{ij} for bismuth[16] yield $\Delta_{Bi}^{el} = 3.8$ eV.

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